What is claimed is:

- 1. A phase and frequency tracking apparatus for multi 2 carrier systems, comprising:
- an mth-order tracking loop for computing a phase
 tracking value, a normalized frequency tracking
 value and a normalized acceleration tracking
 value for a current symbol based on a phase
 estimate of said current symbol and a plurality
 of loop parameters;
- a frequency predictor for calculating as output a feedback compensation frequency for a next symbol based on an equivalent feedback delay, said normalized frequency tracking value and said normalized acceleration tracking value of said current symbol; and
- a pre-DFT synchronizer for compensating the phase and frequency of a received signal in a time domain using said feedback compensation frequency before taking an N-point Discrete Fourier Transform (DFT).
- 2. The apparatus as recited in claim 1 wherein said mth-order tracking loop is a third-order tracking loop modeled with a set of recursive equations, as follows:

$$\phi_{T,i} = \phi_{P,i} + \mu_{\phi,i}\phi_{\varepsilon,i}$$
 $\Omega_{T,i} = \Omega_{P,i} + \mu_{f,i}\phi_{\varepsilon,i}$
 $a_{T,i} = a_{T,i-1} + \mu_{a,i}\phi_{\varepsilon,i}$

5 and

$$\phi_{P,i+1} = \phi_{T,i} + \Omega_{T,i}$$

$$\Omega_{P,i+1} = \Omega_{T,i} + a_{T,i}$$

7 where

- subscript i denotes a symbol index,
- $\phi_{T,i}$, $\Omega_{T,i}$ and $a_{T,i}$ respectively denote said phase, said
- normalized frequency and said normalized
- 11 acceleration tracking values of symbol i,
- $\mu_{\phi,i}$, $\mu_{f,i}$ and $\mu_{a,i}$ respectively denote said loop
- parameters of the ith symbol for $\phi_{T,i}$, $\Omega_{T,i}$ and $a_{T,i}$,
- $\phi_{P,i}$ and $\Omega_{P,i}$ respectively denote a phase prediction
- value and a normalized frequency prediction value
- of the ith symbol,
- $\phi_{P,i+1}$ and $\Omega_{P,i+1}$ are said phase and said normalized
- frequency prediction values of symbol i+1,
- $a_{T,i-1}$ is said normalized acceleration tracking value of
- symbol i-1,
- and $\phi_{arepsilon,i}$, a phase prediction error of the ith symbol, is given
- 22 by:
- $\phi_{\varepsilon,i} = \phi_{E,i} \phi_{P,i}$
- where $\phi_{E,i}$ denotes said phase estimate of the ith symbol.
- 3. The apparatus as recited in claim 2 wherein initial
- 2 values of said phase, said normalized frequency and said
- 3 normalized acceleration tracking values, $\phi_{T,i}$, $\Omega_{T,i}$ and $a_{T,i}$,
- 4 are set to zero, for $i=-1\,;$ said loop parameters $\mu_{f,i}$ and $\mu_{a,i}$
- 5 are equal to zero, for i=0.
- 4. The apparatus as recited in claim 2 wherein said
- 2 feedback compensation frequency is calculated for said next
- 3 symbol from:

$$\Omega_{C,i+1} = \Omega_{T,i} + D_f a_{T,i}$$

- s where D_f is a numerical representation of said equivalent
- 6 feedback delay and $\Omega_{C,i+1}$ is said feedback compensation
- 7 frequency of symbol i+1.
- 5. The apparatus as recited in claim 1 wherein said
- 2 pre-DFT synchronizer receives said feedback compensation
- 3 frequency of the ith symbol, $\Omega_{C,i}$, to compensate the
- 4 frequency of said received signal and de-rotate the phase of
- 5 said received signal in the time domain before taking the
- 6 N-point DFT, by:

$$\widetilde{r_i}[n] = r_i[n] e^{j\Omega_{C,i}\frac{(N-1)-2n}{2N'}}, \quad 0 \le n \le N-1$$

- 8 where n denotes a sample index, $r_i[n]$ denotes said received
- 9 signal of sample n of symbol i, and N^\prime is the number of
- 10 samples in a symbol interval.
- 6. A phase and frequency tracking apparatus for multicarrier systems, comprising:
- an mth-order tracking loop for computing a phase
- tracking value, a normalized frequency tracking
- value and a normalized acceleration tracking
- value for a current symbol based on a phase
- estimate of said current symbol and a plurality
- of loop parameters, wherein said phase tracking
- yalue is employed to compensate for an effect of
- phase drift; and
- a frequency predictor for calculating as output a
- feedback compensation frequency for a next symbol
- based on an equivalent feedback delay, said
- normalized frequency tracking value and said

- normalized acceleration tracking value of said current symbol, whereby pre-DFT synchronization can be accomplished using said feedback compensation frequency.
 - 7. The apparatus as recited in claim 6 wherein said phase estimate of said current symbol, $\phi_{E,i}$, is computed from the following function:

$$\phi_{E,i} = \operatorname{angle}\left(\sum_{m=1}^{N_{SP}} R'_{i,p_m} \left(H_{p_m} X_{i,p_m}\right)^*\right)$$

- 5 where
- superscript * denotes complex conjugation,
- $_{7}$ subscript i denotes a symbol index,
- N_{SP} is the number of the pilot subcarriers,
- 9 subscript p_m denotes a pilot subcarrier index, for
- $m=1\,,\,\ldots\,,\,\,N_{SP}\,\,,$
- H_{p_m} denotes said channel response of pilot subcarrier
- p_m
- $X_{i,p}$ denotes said transmitted data on pilot subcarrier
- p_m of symbol i,
- R'_{i,p_m} denotes said timing compensated version of the *i*th
- symbol on pilot subcarrier location p_m , and
- $\phi_{E,i}$ represents said phase estimate of the ith symbol.
- 8. The apparatus as recited in claim 6 wherein said mth-order tracking loop is a third-order tracking loop
- 3 modeled with a set of recursive equations, as follows:

$$\phi_{T,i} = \phi_{P,i} + \mu_{\phi,i}\phi_{\varepsilon,i}$$

$$\Omega_{T,i} = \Omega_{P,i} + \mu_{f,i}\phi_{\varepsilon,i}$$

$$a_{T,i} = a_{T,i-1} + \mu_{a,i}\phi_{\varepsilon,i}$$

5 and

$$\phi_{P,i+1} = \phi_{T,i} + \Omega_{T,i}$$

$$\Omega_{P,i+1} = \Omega_{T,i} + a_{T,i}$$

7 where

- subscript i denotes a symbol index,
- $\phi_{T,i}$, $\Omega_{T,i}$ and $a_{T,i}$ respectively denote said phase, said normalized
- acceleration tracking values of symbol i,
- $\mu_{\phi,i}$, $\mu_{f,i}$ and $\mu_{a,i}$ respectively denote said loop
- parameters of the ith symbol for $\phi_{T,i}$, $\Omega_{T,i}$ and $a_{T,i}$,
- $\phi_{P,i}$ and $\Omega_{P,i}$ respectively denote a phase prediction
- value and a normalized frequency prediction value
- of the ith symbol,
- $\phi_{P,i+1}$ and $\Omega_{P,i+1}$ are said phase and said normalized
- frequency prediction values of symbol i+1,
- $a_{T,i-1}$ is said normalized acceleration tracking value of
- $_{20}$ symbol i-1,
- and $\phi_{arepsilon,i}$, a phase prediction error of the ith symbol, is given
- 22 by:
- $\phi_{\varepsilon,i} = \phi_{E,i} \phi_{P,i}$
- where $\phi_{E,i}$ denotes said phase estimate of the ith symbol.
- 9. The apparatus as recited in claim 8 wherein initial
- 2 values of said phase, said normalized frequency and said
- 3 normalized acceleration tracking values, $\phi_{T,i}$, $\Omega_{T,i}$ and $a_{T,i}$,
- 4 are set to zero, for i=-1; said loop parameters $\mu_{f,i}$ and $\mu_{a,i}$
- s are equal to zero, for i=0.
- 1 10. The apparatus as recited in claim 8 wherein said
- 2 feedback compensation frequency is calculated for said next
- 3 symbol from:

$$\Omega_{C,i+1} = \Omega_{T,i} + D_f a_{T,i}$$

- 5 where D_f is a numerical representation of said equivalent
- 6 feedback delay and $\Omega_{C,i+1}$ is said feedback compensation
- 7 frequency of symbol i+1.
- 1 11. The apparatus as recited in claim 6 wherein said
- 2 feedback compensation frequency of the ith symbol, $\Omega_{\mathcal{C},i}$, is
- 3 provided as feedback to de-rotate a received signal prior to
- 4 taking the N-point DFT, by:

5
$$\widetilde{r}_{i}[n] = r_{i}[n] e^{j\Omega_{C,i}\frac{(N-1)-2n}{2N'}}, \quad 0 \le n \le N-1$$

- where n denotes a sample index, $r_i[n]$ denotes said received
- 7 signal of sample n of symbol i, and N^\prime is the number of
- 8 samples in a symbol interval.
- 1 12. A phase and frequency drift compensation apparatus
- 2 for multi-carrier systems, comprising:
- a timing offset compensator for receiving a current
- $_{4}$ symbol in a frequency domain after taking an N-
- 5 point Discrete Fourier Transform (DFT) and
- 6 compensating for a timing offset in said current
- 5
 7
 symbol;
- a phase estimator for taking a timing compensated
- yersion of said current symbol on pilot
- 10 subcarrier locations and computing a phase
- estimate for said current symbol based on a
- function of a channel response of each pilot
- subcarrier, transmitted data on each pilot
- subcarrier, and said timing compensated version
- of said current symbol on said pilot subcarrier
- locations;

an mth-order tracking loop for computing a phase tracking value, a normalized frequency tracking value and a normalized acceleration tracking value for said current symbol based on said phase estimate of said current symbol and a plurality of loop parameters;

- a frequency predictor for calculating as output a feedback compensation frequency for a next symbol based on an equivalent feedback delay, said normalized frequency tracking value and said normalized acceleration tracking value of said current symbol;
- a pre-DFT synchronizer for compensating the phase and frequency of a received signal in a time domain using said feedback compensation frequency before taking the N-point DFT; and
- a phase compensator for compensating said timing compensated version of said current symbol for an effect of phase drift with said phase tracking value of said current symbol.
- 1 13. The apparatus as recited in claim 12 wherein said 2 mth-order tracking loop is a third-order tracking loop 3 modeled with a set of recursive equations, as follows:

$$\phi_{T,i} = \phi_{P,i} + \mu_{\phi,i}\phi_{\varepsilon,i}$$

$$\Omega_{T,i} = \Omega_{P,i} + \mu_{f,i}\phi_{\varepsilon,i}$$

$$a_{T,i} = a_{T,i-1} + \mu_{a,i}\phi_{\varepsilon,i}$$

5 and

23

24

25

26

27

28

$$\phi_{P,i+1} = \phi_{T,i} + \Omega_{T,i}$$

$$\Omega_{P,i+1} = \Omega_{T,i} + a_{T,i}$$

7 where

- 8 subscript i denotes a symbol index,
- $\phi_{T,i}$, $\Omega_{T,i}$ and $a_{T,i}$ respectively denote said phase, said
- 10 normalized frequency and said normalized
- acceleration tracking values of symbol i,
- $\mu_{\phi,i}$, $\mu_{f,i}$ and $\mu_{a,i}$ respectively denote said loop
- parameters of the ith symbol for $\phi_{T,i}$, $\Omega_{T,i}$ and $a_{T,i}$,
- $\phi_{P,i}$ and $\Omega_{P,i}$ respectively denote a phase prediction
- value and a normalized frequency prediction value
- of the ith symbol,
- $\phi_{P,i+1}$ and $\Omega_{P,i+1}$ are said phase and said normalized
- frequency prediction values of symbol i+1,
- $a_{T,i-1}$ is said normalized acceleration tracking value of
- symbol i-1,
- and $\phi_{arepsilon,i}$, a phase prediction error of the ith symbol, is given
- 22 by:
- $\phi_{\varepsilon,i} = \phi_{E,i} \phi_{P,i}$
- where $\phi_{E,i}$ denotes said phase estimate of the ith symbol.
- 1 14. The apparatus as recited in claim 13 whereir
- 2 initial values of said phase, said normalized frequency and
- said normalized acceleration tracking values, $\phi_{T,i}$, $\Omega_{T,i}$ and
- 4 $a_{T,i}$, are set to zero, for i=-1; said loop parameters $\mu_{f,i}$ and
- 5 $\mu_{a,i}$ are equal to zero, for i=0.
- 1 15. The apparatus as recited in claim 13 wherein said
- 2 feedback compensation frequency is calculated for said next
- 3 symbol from:
- $\Omega_{C,i+1} = \Omega_{T,i} + D_f a_{T,i}$

- 5 where D_f is a numerical representation of said equivalent
- 6 feedback delay and $\Omega_{C,i+1}$ is said feedback compensation
- 7 frequency of symbol i+1.
- 1 16. The apparatus as recited in claim 12 wherein said
- 2 pre-DFT synchronizer receives said feedback compensation
- 3 frequency of the ith symbol, $\Omega_{\mathcal{C},i}$, to compensate the
- 4 frequency of said received signal and de-rotate the phase of
- 5 said received signal in the time domain before taking the
- 6 N-point DFT, by:

$$\widetilde{r_i}[n] = r_i[n] e^{j\Omega_{C,i}\frac{(N-1)-2n}{2N'}}, \quad 0 \le n \le N-1$$

- 8 where n denotes a sample index, $r_i[n]$ denotes said received
- 9 signal of sample n of symbol i, and N^\prime is the number of
- 10 samples in a symbol interval.
- 1 17. The apparatus as recited in claim 12 wherein said
- 2 phase estimator computes said phase estimate of said current
- symbol, $\phi_{E,i}$, by means of the following function:

$$\phi_{E,i} = \operatorname{angle}\left(\sum_{m=1}^{N_{SP}} R'_{i,p_m} \left(H_{p_m} X_{i,p_m}\right)^*\right)$$

- 5 where
- superscript * denotes complex conjugation,
- 7 subscript i denotes a symbol index,
- N_{SP} is the number of the pilot subcarriers,
- subscript p_m denotes a pilot subcarrier index, for
- $m=1,\ldots,\ N_{SP}\ ,$
- H_{p_m} denotes said channel response of pilot subcarrier
- p_m ,

- X_{i,p_m} denotes said transmitted data on pilot subcarrier p_m of symbol i,
- R_{i,p_m}^\prime denotes said timing compensated version of the ith
- symbol on pilot subcarrier location p_{m} , and
- $\phi_{E,i}$ represents said phase estimate of the *i*th symbol.
- 1 18. A phase and frequency tracking apparatus for multi-2 carrier systems, comprising:
- a pre-DFT synchronizer for compensating the phase and
 frequency of a received signal in a time domain
 using a feedback compensation frequency before
 taking an N-point Discrete Fourier Transform
 (DFT).
- 19. The apparatus as recited in claim 18 wherein said pre-DFT synchronizer receives said feedback compensation frequency of the *i*th symbol, $\Omega_{C,i}$, to compensate the frequency of said received signal and de-rotate the phase of said received signal in the time domain before taking the N-point DFT, by:

$$\widetilde{r_i}[n] = r_i[n] e^{j\Omega_{C,i}\frac{(N-1)-2n}{2N'}}, \quad 0 \le n \le N-1$$

- where n denotes a sample index, $r_i[n]$ denotes said received signal of sample n of symbol i, and N' is the number of
- 10 samples in a symbol interval.